This is the peer reviewed version of the following article: Pappalardo, P., K. Ogle, E.A. Hamman, J. R. Bence, B.A. Hungate, and C.W. Osenberg. 2020. Comparing traditional and Bayesian approaches to ecological meta-analyses. Methods in Ecology and Evolution 11(10):1286-1295. Doi: 10.1111/2041-210X., which has been published in final form at https://doi.org/10.1111/2041-210X.13445. This article may be used for non-commercial purposes in accordance with Wiley Terms and Conditions for Use of Self-Archived Versions. This article may not be enhanced, enriched or otherwise transformed into a derivative work, without express permission from Wiley or by statutory rights under applicable legislation. Copyright notices must not be removed, obscured or modified. The article must be linked to Wiley's version of record on Wiley Online Library and any embedding, framing or otherwise making available the article or pages thereof by third parties from platforms, services and websites other than Wiley Online Library must be prohibited.

ding, fram ted. 1	ing or otherwise making available the article or pages thereof by third parties from platforms, services and websites other than Wiley Online I <b>TITLE:</b> Comparing traditional and Bayesian approaches to ecological meta-analysis
2	
3	RUNNING TITLE: Comparing methods for ecological meta-analysis
4	
5	AUTHORS: P. Pappalardo <sup>1*</sup> , K. Ogle <sup>2,3</sup> , E.A. Hamman <sup>1</sup> , J.R. Bence <sup>5</sup> , B.A. Hungate <sup>3</sup> , and
6	C.W. Osenberg <sup>1</sup>
7	
8	ORCID IDs:
9	Paula Pappalardo: 0000-0003-0853-7681
10	Kiona Ogle: 0000-0002-0652-8397
11	Elizabeth A. Hamman: 0000-0002-3494-6641
12	James R. Bence: 0000-0002-2534-688X
13	Bruce A. Hungate: 0000-0002-7337-1887
14	Craig W. Osenberg: 0000-0003-1918-7904
15	
16	AFFILIATIONS:
17	<sup>1</sup> Odum School of Ecology, University of Georgia, Athens, GA 30602, USA
18	<sup>2</sup> School of Informatics, Computing, and Cyber Systems, Northern Arizona University,
19	Flagstaff, AZ 86011, USA
20	<sup>3</sup> Center for Ecosystem Science and Society and Department of Biological Sciences, Northern
21	Arizona University, Flagstaff, AZ 86011, USA
22	<sup>5</sup> Quantitative Fisheries Center, Department of Fisheries and Wildlife, Michigan State
23	University, East Lansing, MI 48824, USA

- <sup>24</sup> \* Corresponding author contact information: Department of Invertebrate Zoology,
- 25 Smithsonian National Museum of Natural History, Washington, DC 20560, USA, email:
- 26 <u>paulapappalardo@gmail.com</u>, phone: 706-308-2979

- **PAPER TYPE:** Research article
- **KEY WORDS:** bias, confidence interval, coverage, credible interval, effect size, global
- 32 climate change, log response ratio, sample size

### 34 ABSTRACT

- Despite the wide application of meta-analysis in ecology, some of the traditional
   methods used for meta-analysis may not perform well given the type of data
   characteristic of ecological meta-analyses.
- We reviewed published meta-analyses on the ecological impacts of global climate
  change, evaluating the number of replicates used in the primary studies (n<sub>i</sub>) and the
  number of studies or records (k) that were aggregated to calculate a mean effect size.
  We used the results of the review in a simulation experiment to assess the
  performance of conventional frequentist and Bayesian meta-analysis methods for
  estimating a mean effect size and its uncertainty interval.
- 3. Our literature review showed that  $n_i$  and k were highly variable, distributions were 44 right-skewed, and were generally small (median  $n_i$  =5, median k=44). Our 45 46 simulations show that the choice of method for calculating uncertainty intervals was critical for obtaining appropriate coverage (close to the nominal value of 0.95). When 47 k was low (<40), 95% coverage was achieved by a confidence interval based on the 48 t-distribution that uses an adjusted standard error (the Hartung-Knapp-Sidik-49 Jonkman, HKSJ), or by a Bayesian credible interval, whereas bootstrap or z-50 distribution confidence intervals had lower coverage. Despite the importance of the 51 52 method to calculate the uncertainty interval, 39% of the meta-analyses reviewed did 53 not report the method used, and of the 61% that did, 94% used a potentially problematic method, which may be a consequence of software defaults. 54
- 4. In general, for a simple random-effects meta-analysis, the performance of the best
  frequentist and Bayesian methods were similar for the same combinations of factors
  (*k* and mean replication), though the Bayesian approach had higher than nominal

(>95%) coverage for the mean effect when k was very low (k<15). Our literature</li>
review suggests that many meta-analyses that used z-distribution or bootstrapping
confidence intervals may have over-estimated the statistical significance of their
results when the number of studies was low; more appropriate methods need to be
adopted in ecological meta-analyses.

63

# 64 **RESUMEN**

A pesar del uso generalizado del meta-análisis en el área de Ecología, algunos de los
métodos de análisis tradicionalmente utilizados pueden dar resultados no ideales dado
el tipo de datos que los caracteriza.

En este trabajo se realizó una revisión de los meta-análisis publicados sobre los impactos ecológicos del cambio climático global, evaluando el número de réplicas utilizadas en las publicaciones originales (n<sub>i</sub>) y el número de estudios o registros (k) que fueron agrupados para calcular un tamaño de efecto promedio. Se utilizaron los resultados de la revisión en un experimento de simulación para evaluar el desempeño de métodos frecuentistas convencionales y métodos Bayesianos para estimar un tamaño de efecto promedio. y su intervalo de incertidumbre.

753. La revisión de la literatura demostró que  $n_i$  y k fueron muy variables, con76distribuciones sesgadas, y con valores en general bajos (mediana  $n_i$  =5, mediana77k=44). Nuestras simulaciones muestran que la elección del método para calcular un78intervalo de incertidumbre fue crítica para obtener una cobertura apropiada (alrededor79del valor nominal de 0.95). Cuando k fue bajo (<40), obtuvimos una cobertura de</td>8095% utilizando un intervalo de confianza basado en la distribución t de student que81usa un ajuste por el error estándar (llamada Hartung-Knapp-Sidik-Jonkman, HKSJ),

o utilizando un intervalo de credibilidad Bayesiano, mientras que los intervalos de
remuestreo o con una distribución Normal tuvieron cobertura baja. A pesar de la
importancia del método utilizado para calcular el intervalo de incertidumbre, 39% de
los meta-análisis revisados no reportaron el método utilizado y, de los 61% que si lo
reportaron, 94% usaron uno de los métodos potencialmente problemáticos, lo que
puede ser una consecuencia de la configuración por defecto de los programas
informáticos utilizados para meta-análisis.

89 4. En general, para un meta-análisis simple con efectos aleatorios, el desempeño del 90 mejor método frecuentista y el método Bayesiano fueron similares para las mismas combinaciones de factores (k y número de réplicas promedio), aunque el método 91 Bayesiano tuvo cobertura mayor de la nominal (>95%) para el efecto promedio 92 93 cuando k fue muy bajo (k < 15). Nuestra revisión sugiere que muchos de los meta-94 análisis que utilizaron una distribución Normal o intervalos de remuestreo pueden 95 haber sobreestimado la significancia estadística de sus resultados cuando el número 96 de estudios fue bajo. Otros métodos más apropiados deberían ser usados para meta-97 análisis en Ecología.

### 98 INTRODUCTION

99 Meta-analysis uses statistical techniques to quantitatively summarize information from 100 different studies and is highly influential in the contemporary practice of science. To conduct 101 a meta-analysis an investigator gathers summary statistics from each study to calculate an 102 effect size, with the goal of computing an overall effect size (and its uncertainty) and 103 exploring the factors contributing to variation in effect sizes (Nakagawa, Noble, Senior, & 104 Lagisz, 2017). The use of meta-analysis in ecology has been growing rapidly since the 1990s. 105 and has proven particularly useful in discerning general patterns by comparing information 106 from different species, study sites, and systems (Cadotte, Mehrkens, & Menge, 2012). Advice on best methodological practices for meta-analysis is widespread in disciplines with a longer 107 108 history of meta-analytic research (e.g. medical sciences) but is lagging behind in ecology 109 (Gates, 2002). This can be problematic because ecological meta-analyses have specific 110 challenges not necessarily typically in other disciplines.

111 One pervasive characteristic of ecological meta-analyses is the high heterogeneity 112 (i.e., large among-study variation in effect sizes). Senior et al. (2016) analyzed 86 meta-113 analyses in ecology and evolution and found that the among-study variation averaged 92% 114 of the total variance. In contrast, a review of 509 meta-analyses in medicine found that there was no detectable among-study variation in 50% of the studies (Higgins, Thompson, & 115 Spiegelhalter, 2009). Ecological studies also differ from many other disciplines in the typical 116 117 level of within-study replication, which is fewer than 10 replicates per study (Hillebrand & Gurevitch, 2014). Such low levels of replication will influence the precision of the estimates 118 119 of effect size from the primary studies (Langan, Higgins, & Simmons, 2016). Importantly, 120 the low level of replication typical of ecological studies is outside the range used in most 121 simulation studies designed to assess meta-analytic methods, which typically range from dozens to hundreds (Langan et al., 2016). Thus differences between ecology and other
disciplines potentially limit the insights ecologists can gain from existing simulations that
compare different meta-analytic methods.

125 Specific advice for conducting ecological meta-analyses include suggestions on the 126 type of meta-analytic model and effect size calculation to use (Gurevitch & Hedges, 1999; 127 Osenberg, Sarnelle, Cooper, & Holt, 1999; Lajeunesse, 2015), and how to deal with nonindependence (Gurevitch & Hedges, 1999; Noble, Lagisz, O'dea, & Nakagawa, 2017; Song, 128 Peacor, Osenberg, & Bence, 2020). For example, a random-effects model is often 129 130 recommended for ecological meta-analysis over a fixed-effects model (Gurevitch & Hedges, 1999), and multi-level models are increasingly being used to incorporate the non-131 132 independence commonly found in ecological meta-analyses (Nakagawa & Santos, 2012). A topic addressed in the medical literature that has received little attention in ecology (but see 133 134 Adams, Gurevitch, & Rosenberg, 1997) is the choice of confidence interval (CI) used to 135 estimate the mean effect size in a meta-analysis (Hartung & Knapp, 2001; Sidik & Jonkman, 136 2003, Sánchez-Meca & Marín-Martínez, 2008).

Simulation studies have shown that when the number of studies (k) in the meta-137 analysis is low, the CIs for a mean effect size calculated using a normal approximation are 138 139 too narrow, leading to coverage below the nominal level (i.e., a 95% CI should include the 140 true value 95% of the time) (Brockwell & Gordon, 2001; Sánchez-Meca & Marín-Martínez, 141 2008). To avoid this problem, meta-analyses in the medical literature often use the HKSJ 142 (Hartung-Knapp-Sidik-Jonkman; Hartung & Knapp, 2001; Sidik & Jonkman, 2003) method, which is based on a *t*-distribution and can achieve good coverage even when k is small 143 (Inthout, Ioannidis, & Borm, 2014). Bootstrap techniques have been recommended for 144 145 estimating CIs for means in ecological meta-analyses, due to its robustness to departures from normality (Adams et al., 1997). On the other hand, boot-strapped CIs can lead to poorcoverage when estimating the among-study variance (Viechtbauer, 2007).

148 Bayesian methods, and the credible interval, offer an alternative approach to 149 estimating uncertainty in meta-analyses. Although Bayesian methods may have a steep 150 learning curve, they offer advantages in handling hierarchical models, for incorporating prior information, and for dealing with missing data (Ogle, Barber, & Sartor, 2013). Bayesian 151 152 meta-analytic techniques produce a posterior distribution of the mean effect size and associated variance terms. Estimates of uncertainty, including credible intervals, can be 153 154 directly obtained from the posterior distributions, offering an easier to interpret alternative to 155 the frequentist-based CI (Kruschke & Liddell, 2008).

156 Our main goal is to compare the performance of traditional and Bayesian methods to 157 measure the uncertainty around the estimation of a mean effect in the context of ecological 158 meta-analysis. To achieve this goal, we conducted a two-pronged study. First, we reviewed 159 published ecological meta-analyses to characterize the types of confidence interval used in 160 ecological meta-analyses, the number of replicates used in the primary studies  $(n_i)$  included in published meta-analyses, and the number of studies (k) that were aggregated to calculate 161 162 a mean effect size. Second, we used the  $n_i$  and k found in our literature review to inform the 163 range of parameter values to use in conducting simulation experiments relevant to ecological meta-analyses. In particular, we determined the typical levels of  $n_i$ , k, and the among-study 164 165 variance and then varied them systematically in our simulation studies. We then evaluated performance of frequentist and Bayesian meta-analysis methods when applied to the 166 167 simulated data, especially with respect to their ability to estimate the true mean effect and 168 among-study variance, and their quantification of uncertainty intervals (i.e., confidence or 169 credible intervals). Based on our findings, we generate recommendations on the methods to measure uncertainty that perform best for ecological meta-analysis and highlight how simple
choices (sometimes overlooked by the investigators) can affect the results of meta-analyses.

**173 MATERIALS AND METHODS** 

#### 174 Literature review to assess characteristics of ecological datasets

175 Literature search. We searched the Core Collection of the ISI Web of Science database in March 2017; the search string for TOPIC included (["meta-analy"" OR "metaanaly"" OR 176 "meta analy\*"] AND ["climate change" OR "global change"]). We only included articles 177 178 and reviews within the "Ecology", "Environmental Sciences", "Biodiversity Conservation" 179 and "Plant Sciences" categories. The search resulted in 581 citations; the PRISMA diagram 180 detailing the screening process is provided in Figure S1. After abstract screening, we checked 181 the full text of the 205 articles published between 2013 and 2016. Of these, 96 papers satisfied 182 the inclusion criteria for the final analysis.

183 **Criteria for inclusion.** We focused on narrow sense meta-analyses: i.e., those that used a quantitative meta-analytic method to combine effect sizes that compared a control and a 184 185 treatment group. We excluded studies that 1) only cited published meta-analyses, 2) reviewed 186 meta-analytic methods, but did not perform a meta-analysis, 3) were identified as meta-187 analysis by the authors but did not use a meta-analytic model or did not calculate effect sizes, 4) used the correlation between two variables as an effect size, and 5) were not "biological 188 meta-analyses" (as defined in Nakagawa et al., 2017), such as studies related to human health 189 or human behavior. 190

191 **Information extracted.** For each paper we extracted the number of studies (k) from the text, 192 figure captions, figures, and supplementary materials. Here we define a "study" as yielding 193 an estimate of an effect, so that a given primary paper could generate multiple effects and 194 thus multiple studies. The k values were determined at three levels, 1) overall: i.e., the total 195 k collected by the authors (e.g., if they conducted meta-analyses on different response 196 variables, then we summed the k across these variables); 2) analysis: i.e., the total k used in 197 a particular analysis (e.g., if an analysis examined variation among four levels of a moderator, 198 then we summed up the number of studies in each level); and 3) category: i.e., the k included 199 in each category of a categorical analysis. In some cases, authors calculated mean effect sizes for different categories separately and only compared the categories using confidence 200 201 intervals (i.e., there was no integrated analysis incorporating a category effect). In this case, 202 we considered each's categories' k to apply at the "analysis" level.

When available, we also recorded the number of replicates  $(n_i)$  in the original studies. If the level of replication was unequal for the control and treatment groups, we recorded the average. Finally, from each meta-analysis, we also recorded the inferential paradigm used (frequentist vs. Bayesian) and the method used to obtain confidence intervals for the frequentist approaches (e.g., non-parametric bootstrap, normal-based, KHSJ, etc.).

# 208 Simulation Experiments

215 0.25, 0.5, 1, 2, 5}. We simulated 2,000 replicated meta-analyses for each combination of *n*, 216 *k*, and  $\sigma_{among}^2$ . We then evaluated the performance of four meta-analytic methods applied to 217 the simulated data: three frequentist approaches that differed in how they calculated 218 confidence intervals for a mean effect and a Bayesian approach.

219 Simulating raw data for a study. We first determined the number of replicates for study *i* 220  $(n_i)$  based on a random draw from a Poisson distribution:

$$n_i^* \sim Poisson(n-2)$$
 (Eq. 1)

$$n_i = n_i^* + 2 \tag{Eq. 2}$$

where *n* is the mean number of replicates representative of ecological meta-analyses. We subtracted 2 to sample from the Poisson and added 2 to the simulated  $n_i^*$  to make the minimum number of replicates for each simulated study equal 2 rather than 0. For each study, we assumed equal number of replicates for the control and treatment groups.

Individual observations  $(j = 1, 2, ..., n_i)$  for the control and treatment groups were generated from a lognormal distribution (*LN*) such that for study *i* and observation *j*:

227 
$$y_{C_{ij}} \sim LN(0, \sigma_{rep}^2)$$
(Eq. 3)

228 
$$y_{T_{ij}} \sim LN(0 + \mu + \varepsilon_i, \sigma_{rep}^2)$$
(Eq. 4)

where  $\sigma_{rep}^2$  is the among-replicates variation,  $\mu$  is the true overall effect, and  $y_{C_{ij}}$  and  $y_{T_{ij}}$ are the simulated observations for study *i* and observation *j* of the control and treatment group, respectively. We set the among-replicate variation equal to 1 for both the control and treatment. For convenience, we set the location parameter for the control group equal to zero, resulting in median ( $y_c$ ) = 1. For the treatment group in study *i*, we set median ( $y_T$ )=  $\mu + \varepsilon_i$ , where  $\mu$  is the overall true treatment effect (hereafter, true effect size) and  $\varepsilon_i$  is the random effect associated with study *i*. We simulated  $\varepsilon_i$  as:

$$\varepsilon_i \sim N(0, \sigma_{among}^2)$$
 (Eq. 5)

Thus, the true effect size from any given study departs from  $\mu$  due to its random effect (determined by  $\varepsilon_i$ ), while the estimated effect size differs from the true effect size due to within-study sampling error (i.e., as influenced by  $n_i$  and  $\sigma_{rep}^2$ ). The range of values used for  $\sigma_{among}^2$  were chosen to produce a similar distribution of  $I^2$  (the proportion of variation among effect sizes not explained by sampling error) to that reported by Senior et al. (2016) for metaanalyses in ecology and evolution ( $I^2$  simulation results are presented in Figure S2).

Estimating the effect size and within-study variance. Using the raw data simulated from each study, we computed the observed effect size for study *i* as the log response ratio ( $lnRR_i$ ), which is widely used in ecology (Nakagawa & Santos, 2012) and it is often a reasonable approximation of ecological phenomena (Osenberg, Sarnelle, & Cooper, 1997):

247 
$$lnRR_i = ln\left(\frac{\bar{y}_{T_i}}{\bar{y}_{C_i}}\right)$$
(6)

where  $\bar{y}_{T_i}$  and  $\bar{y}_{c_i}$  are the sample means of the treatment and control groups, respectively. The expected sample means for each treatment in a simulated study are  $E\left(y_{c_{ij}}\right) = \exp\left(\frac{\sigma_{rep}^2}{2}\right)$  and  $E\left(y_{T_{ij}}\right) = \exp\left(\mu + \varepsilon_i + \frac{\sigma_{rep}^2}{2}\right)$ . Thus, the log of the ratio of the expected values for the treatment and control groups is  $\mu + \varepsilon_i$ , corresponding to what we call the true study-specific effect size.

253 We calculated the estimated within-study variance of the log ratio (Eq. 1 in Hedges, 254 Gurevitch, & Curtis, 1999) ( $\sigma_{within_i}^2$ ) as:

255 
$$\sigma_{within_{i}}^{2} = \frac{SD_{T_{i}}^{2}}{n_{T_{i}}\cdot\bar{y}_{T_{i}}^{2}} + \frac{SD_{C_{i}}^{2}}{n_{C_{i}}\cdot\bar{y}_{C_{i}}^{2}}$$
(7)

where  $SD_T$  and  $SD_C$  are the sample standard deviations of the treatment and control groups, respectively, and  $n_{T_i} = n_{C_i} = n_i$  are the simulated number of replicates in study *i*.

258

# 259 Meta-analytic approaches

Given that we simulated independent data to highlight how the choice of uncertainty interval affects the estimation of a mean effect, we used a standard random-effects model (Gurevitch & Hedges, 1999). We comment on how our results may change with a multi-level (hierarchical) model in the Discussion section. We assume the simulated effect size for study *i* (*lnRR<sub>i</sub>*, calculated from Eq. 6) follows a normal distribution with mean  $\theta_i$  (the true effect for study *i*) and within-study variance  $\sigma_{within_i}^2$ :

266 
$$lnRR_i \sim N(\theta_i, \sigma_{within_i}^2)$$
 (8)

267 
$$\theta_i \sim N(\mu, \sigma_{among}^2)$$
 (9)

We assume  $\sigma_{within_i}^2$  is known, as calculated via Eq. 7. Likewise, the true study-specific effect size,  $\theta_i$ , is assumed to follow a normal distribution with mean  $\mu$  (the true overall effect) and among-study variance,  $\sigma_{among}^2$  (which is sometimes referred to as  $\tau^2$  in other meta-analytic papers).

We compared different methods to construct confidence intervals (CIs) for a mean effect (at the analysis level) within the frequentist methods versus Bayesian credible intervals. For the frequentist-based analyses, we compared: a) a CI based on a *z*-distribution, which is a large sample approximation, b) a weighted CI based on the Hartung-Knapp-Sidik-Jonkman (HKSJ) method, which does not assume a large sample and instead uses a *t*- distribution, and c) bootstrap methods. For the Bayesian-based analysis, we calculated thehighest posterior density (HPD) credible interval.

279 Frequentist approaches. We applied the random-effects model described by Eqs. 8 and 9 with inverse variance weights using the "rma" function in the R package metafor 280 (Viechtbauer, 2010), and estimated  $\sigma^2_{among}$  with the default REML method. To calculate the 281 282 z-distribution CI, we used the default settings for the random-effects model in *metafor*, which 283 returns a 95% CI for  $\mu$  based on the normal distribution. To apply the HKSJ CI, we set the 284 option knha=T in *metafor*. The resulting CI for  $\mu$  is based on both a refined estimate of  $\sigma^2_{among}$  and a Student's t-distribution (Hartung & Knapp, 2001; Sidik & Jonkman, 2003), 285 which accounts for the fact that  $\sigma^2_{among}$  is estimated and not known. For the bootstrapped CI, 286 we estimated the bias-corrected non-parametric bootstrapped 95% CI for both  $\mu$  and  $\sigma^2_{among}$ 287 via the boot package in R (Canty & Ripley, 2017). Since the choice of HKSJ or z-distribution 288 for the  $\mu$  CI does not affect the estimation of  $\sigma_{among}^2$ , in both cases we used *metafor*'s 289 function "confint" to obtain the CI for  $\sigma^2_{among}$  ("confint" applies a Q-profile method in 290 291 combination with REML).

Bayesian approach. We used a "hybrid" Bayesian framework to implement the randomeffects model (Eqs. 8 and 9) in which we treat  $\sigma_{within}^2$  as known; whereas a fully Bayesian model may treat  $\sigma_{within}^2$  as unknown (this hybrid model is comparable to the "empirical Bayes" method discussed in Schmid & Mengersen, 2013). Initial explorations with full and hybrid models gave qualitatively similar results and we only include the hybrid model in our analysis. We specified relatively non-informative priors for the unknown quantities (e.g.,  $\mu$  and  $\sigma_{among}^2$ ). For the mean effect size,  $\mu$ , we specified a conjugate normal prior with a mean of zero and large variance: N(0, 10000). Given that even diffuse priors for  $\sigma_{among}^2$  can influence the posterior for  $\sigma_{among}^2$ , particularly under small group size (Gelman, 2006), we explored five different priors for  $\sigma_{among}^2$  (Supporting Information Figures S12-15). For the final analysis, convergence statistics and computational speed led us to focus on the *Uniform*(0,10) prior for the standard deviation ( $\sigma_{among}$ ).

The Bayesian meta-analyses were implemented in JAGS with the riags R package 305 (Plummer, 2018). For each model, we ran three parallel Markov chain Monte Carlo (MCMC) 306 sequences for 200,000 iterations, and discarded the first 100,000 iterations as the burn-in 307 period. We used the  $\hat{R}$  convergence diagnostic (Gelman & Rubin, 1992) to evaluate 308 convergence of the MCMC sequences to the posterior. For the final simulations, we only 309 included runs that had  $\hat{R} < 1.1$ , and checked that the proportion of discarded runs was lower 310 than 1%. Using post-burn-in MCMC samples, we computed posterior means for quantities 311 of interest (e.g.,  $\mu$  and  $\sigma^2_{among}$ ) as point estimates. We computed 95% credible intervals as 312 HPD intervals for both  $\mu$  and  $\sigma^2_{among}$  using the "HPD interval" function in the *coda* package 313 314 (Plummer, 2006).

# 315 Implementation and Assessment of the Meta-analysis Approaches

We ran all the analyses and simulations in the R environment (R Core Team, 2019); code is provided in the Supporting Information. For each simulated dataset, we estimated  $\mu$  and  $\sigma_{among}^2$  via the frequentist and Bayesian methods described above. We summarized the results from the 2,000 replicated meta-analyses for each combination of factors  $(n, k, \sigma_{among}^2)$  and modeling approaches (i.e., frequentist and Bayesian methods to measure uncertainty). The results for the model performance associated with estimating  $\sigma_{among}^2$  are presented in Figures S7-10.

We evaluated model performance using: coverage, width of the uncertainty intervals, bias, and efficiency. We estimated *coverage* for both  $\mu$  and  $\sigma_{among}^2$  as the proportion (out of the 2,000 simulation replicates) of calculated 95% uncertainty intervals (CIs for the frequentist methods and credible interval for the Bayesian approach) that included the corresponding true value. Ideally, coverage should equal the nominal value of 0.95 (95%). CIs for these "coverage proportions" were computed using the "binom.confint" function in the R *binom* (Sundar, 2014) package, with the method "wilson" (Agresti & Coull, 1998).

We summarized the perceived uncertainty for  $\mu$  and  $\sigma_{among}^2$  as the mean width of the 95% uncertainty intervals for the 2,000 intervals for each scenario, and assessed how well the mean width was estimated using a 95% CI based on a *t*-distribution. All else being equal, smaller uncertainty is a desirable feature, but not if it is accompanied by a reduction in coverage below the nominal level.

To evaluate *bias*, we calculated the mean difference between the point estimates for  $\mu$  and  $\sigma_{among}^2$  and their true values based on the 2,000 simulation replicates, and report a 95% CI for this estimate based on the *t*-distribution. Ideally, bias should be centered on zero. Finally, to quantify the *efficiency* of the point estimates, we calculated the root mean squared error (RMSE) between the estimated and true values for  $\mu$  and  $\sigma_{among}^2$  as:

340 
$$RMSE = \sqrt{\frac{\sum_{s=1}^{N_{sim}} (\hat{a}_s - a_{true_s})^2}{N_{sim}}},$$
 (10)

341 where  $a = \mu$  or  $\sigma_{among}^2$ ,  $\hat{a}$  is the point estimate from each model,  $a_{true}$  is the true value used 342 in the simulations, and  $N_{sim}$  is the number of simulations.

343

#### 344 **RESULTS**

# 345 Literature review to assess characteristic of ecological datasets

346 Of the 96 meta-analyses that satisfied our criteria (Table S1), 95 and 26 provided information on the number of studies (k) and number of replicates  $(n_i)$  associated with the original dataset, 347 respectively. Only three meta-analyses used a Bayesian approach. The majority of meta-348 349 analyses were published in *Global Change Biology* (23), followed by *Agriculture Ecosystems* 350 & Environment (7) and Ecology (6) (Figure S3 displays the full list). The quality of reporting 351 varied, and is discussed in more detail in the Supporting Information. We also provide additional information on k and  $n_i$  (by taxa, environment, and topic) in the Supporting 352 353 Information (Table S2, Figures S4-S5).

354 **Number of studies**. The number of studies (k) used to estimate an effect was highly skewed at the three levels we considered: overall, analysis, and category (Figure 1). The overall k355 ranged from 25 to 32,567 (Figure 1A upper panel), with a median of 273 and with relatively 356 few (12%) including more than 1,000 studies. For most papers, however, analyses were 357 performed for different response variables or different moderators, and the k used for a 358 particular analysis was considerably lower (Figure 1A middle panel), ranging from k = 1 (for 359 a paper that presented all possible comparisons, even when one potential analysis was 360 represented by only a single study) to k = 8,474, with a median of k = 44 (i.e., 50% of meta-361 analysis included 44 or fewer studies); 16% had  $k \le 10$ . The number of studies included 362

within categories ranged from k = 1 to 1,430, with a median of 16; 36% had  $k \le 10$  (Figure 1A lower panel).

Number of replicates. The distribution of the reported number of replicates in the original studies  $(n_i)$  cited by the climate change meta-analyses was highly skewed, ranging from  $n_i =$ 1 to 21,600, with most studies having only a few replicates; the median was 5 (Figure 1B). The strong skewness in these data led us to inspect some of the original publications from which exceptionally large  $n_i$  values were reported. We found publications in which  $n_i$  values were likely misreported or greatly inflated by pseudoreplication (details in Table S3 and Figure S6).

Analytic method to estimate the uncertainty interval for a mean effect. In 38.5% of the 372 papers reviewed, the method used to calculate the frequentist-based CI for the mean effect 373 374 was not mentioned (Figure 2). Of the papers reporting how the CI was calculated, the 375 majority used bootstrapped or z-distribution CIs; only three papers used credible intervals 376 (Bayesian method), and a few used a combination of methods (Figure 2). No papers reported 377 using HKSJ method. Of the papers that did not specify the method, nine used Metawin (which defaults to a *t*-distribution for the parametric CI, without the KHSJ refinement); 12 papers 378 used the packages meta or metafor in R (which default to a z-distribution); and two used the 379 Comprehensive Meta-Analysis software (which defaults to a z-distribution). Assuming these 380 381 23 papers used the software defaults, then 31 papers used a z-distribution, and nine used a tdistribution but without the KHSJ refinement. Thus, bootstrapped and z-distribution CIs 382 383 likely comprise the vast majority of approaches, with KHSJ CIs being entirely absent from 384 our dataset.

### 386 Simulation experiments: estimation of a mean effect

The number of studies, k, used to estimate a mean effect size,  $\mu$ , substantially affected the 387 coverage of the frequentist methods, but this effect of k depended on the type of method used 388 389 to estimate the 95% CIs (Figure 3A). For example, z-distribution CIs for  $\mu$  had coverage lower than the nominal level when k < 40, and coverage was appreciably lower for k < 20390 391 (Figure 3A). Similarly, bootstrapped CIs had lower than nominal coverage when k < 40392 (Figure 3A). In contrast, KHSJ CIs had close to nominal coverage over all values of k (Figure 393 3A). The Bayesian credible interval generally showed coverages around 95%, but when k =5, coverage was >95% (Figure 3A). 394

395 Coverage can be smaller than nominal levels either because of bias or because the 396 width of the uncertainty interval is inappropriately narrow (i.e., uncertainty is underestimated). The three frequentist methods for computing CIs for  $\mu$  used the same 397 398 approach for obtaining point estimates and had minimal bias centered on zero (Figures S11 399 A,C,E). Thus, the observed differences in coverage for  $\mu$  resulted from differences in the 400 width of the uncertainty interval (Figure 3B). The Bayesian credible interval was generally 401 wider than the frequentist-based CIs, and of the frequentist CIs, the KHSJ CI tended to be the widest; when k was small, the z-distribution and boot-strapped CIs were  $\sim 1/3$  smaller than 402 403 they should be based upon the more appropriate KHSJ CI (Fig. 3B).

Increasing the mean number of replicates (*n*) in the primary studies did not greatly affect coverage (Figure 3B), the width of the uncertainty interval (Figure 3E), bias (Figure S11C), or RMSE (Figure S11D) for  $\mu$ . Our results were likely produced because the amongstudy variation dominated within-study variation over the range of levels considered for the simulation factors (as determined by the review by Senior et al., 2016). 409 Increasing the among-study variance  $(\sigma_{among}^2)$  increased the width of the uncertainty 410 interval for  $\mu$  (Figure 3F), but had only small effects on coverage (Figure 3C). Bias in the 411 estimation of  $\mu$  was negligible and unaffected by an increase in  $\sigma_{among}^2$  (Figure S11E), but 412 the error in the estimation increased with the increase in heterogeneity (RMSE, Figure S11F).

413

#### 414 **DISCUSSION**

415 Our literature review shows that ecological meta-analyses are highly variable in terms 416 of how many studies (k) are included in the meta-analysis and the number of replicates reported in the original publications  $(n_i)$ . Despite this high variability, both across and within 417 418 meta-analyses, k and  $n_i$  tend to be low. The high frequency of meta-analyses with comparatively few studies ( $k \le 44$  in 50% of meta-analyses reviewed) is not unique to 419 420 ecology; even lower number of studies are pervasive in medical research (Kontopantelis, 421 Springate, & Reeves, 2013) where there has been an effort to develop methods that improve 422 the performance of meta-analyses in such scenarios (Inthout et al., 2014). Furthermore, our simulations show that the method used to calculate an uncertainty interval greatly influences 423 424 how often the interval includes the true mean effect and is very important for producing 425 intervals with close to correct coverage when k is low. Despite its importance, a large proportion of the ecological meta-analyses we reviewed (38%) did not report the type of 426 uncertainty interval used, and the ones that did report their methods used intervals that are 427 428 problematic when k is low.

Low coverage of the z-distribution confidence interval (CI) when the number of observations (in the meta-analysis context, the number of studies, *k*) are low is well known in classical statistical contexts as well as in meta-analyses (Hedges et al., 1999; Brockwell &

Gordon, 2001; IntHout et al., 2014). In meta-analyses, however, approaches typically default to assuming large k and thus justify the application of the *z*-distribution. In ecology, this large-sample approach is often unwarranted (Figure 1A). Furthermore, bootstrapped CIs are also well known to be problematic with small k (Hesterberg, 2015), although ecological metaanalyses tend to prioritize the potential for non-normal distributions over concerns about small k (Adams et al., 1997) – based upon our results, such prioritization may be misplaced.

438 When k is low, the CI for a mean effect size ( $\mu$ ) based on the z-distribution is too narrow. Some practitioners have addressed this problem by not calculating CIs when k is 439 440 very small (e.g.: Augusto, Delerue, Gallet-Budynek, & Achat, 2013). Others have resorted 441 to using bootstrapped CIs (e.g.: Thébault, Mariotte, Lortie, & MacDougall, 2014). Given that 442 bootstrapped CIs also had poor coverage when k < 40, this approach appears to be ill-advised. 443 In our review, nearly half of the mean effect sizes used in an individual analysis were 444 calculated with k < 40 effect sizes, where the choice of method for computing uncertainty 445 intervals matters. As a result, many effects declared as significant probably should not have 446 been. This is exemplified in a review of medical meta-analyses from the Cochrane Database, 447 where of the 315 meta-analyses that yielded significant effects with the z-distribution CI, 448 only 79 were significant using the HKSJ CI (Inthout et al., 2014).

The default option for frequentist CIs for  $\mu$  varies among software packages. For example, a *t*-distribution CI (but without the HKSJ refinement) is Metawin's default, whereas the *z*-distribution is the default in the Comprehensive Meta-Analysis software and in the R packages *meta* and *metafor* (metafor is one of the most common software packages currently in use by ecologists). For those planning to conduct a random-effects meta-analysis using frequentist methods, we advise use of the HKSJ CI, which employs both a weighted estimator of the variance for the overall effect size and a *t*-distribution for its associated CI (this can be 456 set up in *metafor* using the option knha= T). Sánchez-Meca and Marín-Martínez (2008) 457 report that the HKSJ method outperforms the simple CI-based on the *t*-distribution. However, 458 in some scenarios, coverage could be as low as 90% even using the HKSJ CI, for example, 459 when heterogeneity is high, k < 10, and the number of replicates varies greatly among studies 460 (Inthout et al., 2014). In our simulations that did not include highly uneven number of 461 replicates, we showed that HKSJ CI's and the Bayesian credible intervals provide accurate 462 (or at least conservative, >95%) coverage and performed best. We encourage researchers to 463 be aware of the software defaults when calculating an uncertainty interval, and to report the 464 method used.

The climate change meta-analyses showed exceedingly high variation in the number 465 of replicates reported  $(n_i)$ , spanning five orders of magnitude, but the majority of values were 466 467 low. In fact,  $n_i < 10$  in 67% of the cases, and  $n_i \le 5$  in 51% of the cases we reviewed. This 468 pattern may be similar in other fields of ecology (Table S2, Figures S4, S5). For example, a 469 competition meta-analysis found  $n_i$  ranging from 1 to 1,455, with a median of 10 (Gurevitch 470 et al., 1992). To obtain a more accurate estimate of  $\mu$ , some authors specify a minimum  $n_i$  to 471 calculate mean effect sizes (Gurevitch et al., 1992; Schirmel et al., 2016). Such censuring 472 might improve confidence interval performance by reducing variation in replication among studies (Inthout et al. 2014) but at the high cost of discarding important information. While 473 474 one would in general expect better estimates with more replication, our simulation 475 experiment did not show important effects of the mean number of replicates on the estimation 476 of and inferences about  $\mu$ . A similar insensitivity to the number of replicates has been observed in other studies (Sánchez-Meca & Marín-Martínez 2008), although we included 477 fewer replicates than most other simulations. Variation in replication among studies, should 478 produce variation in within-study variance, especially when the number of replicates is small. 479

However, in our simulations among-study variation was much larger than within-study
variation, consistent with the characteristics of ecological meta-analyses (Senior et al., 2016),
minimizing the role of variation in the number of replicates.

When the number of replicates reported  $(n_i)$  was unusually high, we checked a few 483 of the original papers cited in each meta-analysis. Upon revisiting 17 of the original 484 publications, we found at least 15 cases in which  $n_i$  was misreported (Table S3). This 485 manifested in different ways. Some meta-analyses reported the total  $n_i$  in an experiment 486 487 instead of the number of replicates per treatment. In other cases, authors reported the total  $n_i$ 488 from repeated measurements or the numbers of individuals rather than the number of true 489 replicates (e.g., plots or cages). There were also cases in which we were unable to verify the origin of the number reported in the meta-analysis. An incorrect  $n_i$  decreases the sampling 490 variance for that effect size, which affects the weights and also the estimation of the overall 491 492 heterogeneity (Noble et al., 2017). Researchers conducting a meta-analysis should be 493 cautious when extracting data from the original studies to avoid misreporting (or inflating) 494 the number of replicates. Publication of the data and code used to conduct a meta-analysis would also be useful to inform research on best practices for meta-analysis. 495

In our simulations using a random-effects model, the performance in the estimation 496 of the among-study variance  $(\sigma_{among}^2)$  was better when the true  $\sigma_{among}^2$  was high (Figures 497 S4-7). In agreement with Viechtbauer (2007), we observed that the Q-profile CI method for 498  $\sigma_{among}^2$  performed better than the bootstrap method (Figures S7-10). The Bayesian method 499 performed best, but had coverage above the nominal level when the number of studies was 500 501 low (k < 20). Bayesian methods led to higher perceived uncertainty in such cases, which could be real, but this could also be a consequence of positive bias in the  $\sigma^2_{among}$  estimates, 502 which was more pronounced for the Bayesian methods when k < 20. In this scenario, one 503

approach to improve coverage is to use priors for  $\sigma_{among}^2$  that perform better when k is low (Gelman, 2006). Another solution is to specify more informative priors for  $\sigma_{among}^2$  based on a synthesis of past publications (Higgins et al., 2009). One reason to desire good estimation of  $\sigma_{among}^2$  is because overestimation of this variance component can lead to higher perceived uncertainty in the estimate of  $\mu$ . An additional reason is that the estimates of  $\sigma_{among}^2$  represent real variation in effects and could be of importance in risk assessment.

In the initial explorations with the full Bayesian model, the MCMC chains for  $\mu$ 510 converged quickly, but they converged more slowly for  $\sigma^2_{among}$ , often falling into a "zero 511 variance trap" (Gelman, 2004) when the true among-study variance was close to zero. In 512 general, convergence and mixing problems were most frequent for low k and low  $\sigma_{among}^2$ . 513 While low  $\sigma^2_{among}$  is rare in ecology, low k is not. Of the priors we explored (Supporting 514 Information Figures S12-15), the folded-*t* and the uniform prior for the standard deviation 515 516 performed best when k was low (we chose the uniform prior for the final simulations because 517 it ran slightly faster). In our simulations, the hybrid Bayesian model exhibited the practical 518 advantages of the Bayesian methods (e.g., produces full posteriors and direct evaluation of 519 uncertainty without approximating assumptions, among others), and was easy (and faster) to 520 implement than the full model. On the other hand, a full Bayesian approach may be more useful for multi-level models that include missing data, hierarchical structures, and/or 521 covariate effects (Ogle et al., 2013), and could benefit from informative priors for  $\sigma_{among}^2$ , 522 particularly when k is low. 523

524 Our study simulated independent effect sizes. Often though, observed effect sizes are 525 not independent (e.g., multiple observed effect sizes might be obtained from a single 526 published article). As observed effect sizes within a group might respond similarly (due to 527 similar methods, or similar environmental conditions), some of the among-study variation 528 could be common to all members of a group or subgroup. Multi-level (hierarchical) models 529 can be used to account for this. We believe that our results, including the insensitivity of our 530 results to *n*, would not be materially altered in such situations, assuming the among-study 531 variation still dominates the within-study variation. There are some challenges to be faced, 532 however, when applying our results to more complex multi-level models. In particular, 533 although the R package *metafor* has a function that handles multi-level models (rma.mv), the 534 KHSJ adjustment is not available in this context, and the best that can be done with metafor 535 is to construct *t*-based confidence intervals of the mean (also referred to as conditional *t*-test). For multi-level models, these *t*-based confidence intervals have inflated error rates (Luke, 536 2017; Song et al., in press), although they do outperform normal-based confidence intervals 537 538 (Song, personal communication). Song et al. (in press) speculated that the inflated error rates 539 of t-based confidence intervals resulted from not accounting for uncertainty in estimated 540 variances. Methods exist for adjusting tests and confidence intervals to account for 541 uncertainty in estimated variances in multi-level models, such as the Kenward-Rogers 542 adjustment, or simulation of null distributions (Halekoh & Hojsgaard, 2014), but to our 543 knowledge these have not been implemented in any readily available software for conducting 544 meta-analyses.

545

### 546 AUTHORS CONTRIBUTIONS

All authors conceived the idea; PP collected and analyzed the data with contributions from
CWO, EAH, JRB, and KO. PP led the writing; all authors contributed critically to the drafts
and gave final approval for publication.

550

## 551 DATA AVAILABILITY

The data compiled in the literature review, the R code for the simulation experiment, and the results from the simulation experiments are deposited in Dryad repository: https://doi.org/10.5061/dryad.zw3r22863.

555

#### 556 ACKNOWLEDGMENTS

This research was funded by the U.S. Department of Energy (DE-SC-0010632), National Science Foundation (DEB-1655426 and DEB-1655394), and utilized Georgia Advanced Computing Resource Center resources. This is publication 2020-17 of the Quantitative Fisheries Center. We thank W. Viechtbauer for feedback on *metafor* computations, Natasja vanGestel and Kees Jan vanGroenigen for feedback during early stages of the project, Chao Song for helpful discussion, and Sergio Estay for his feedback on the abstract in Spanish.

563

#### 564 **REFERENCES**

- Adams, D. C., Gurevitch, J., & Rosenberg, M. S. (1997). Resampling tests for metaanalysis of ecological data. *Ecology*, 78(4), 1277. https://doi.org/10.2307/2265879
- Agresti, A., & Coull, B. A. (1998). Approximate is better than "exact" for interval
  estimation of binomial proportions. *The American Statistician*, 52(2), 119–126.
  https://doi.org/10.1080/00031305.1998.10480550
- 570 Augusto, L., Delerue, F., Gallet-Budynek, A., & Achat, D. L. (2013). Global assessment of
- 571 limitation to symbiotic nitrogen fixation by phosphorus availability in terrestrial
- 572 ecosystems using a meta-analysis approach. *Global Biogeochemical Cycles*, 27(3),
- 573 804–815. https://doi.org/10.1002/gbc.20069

574	Brockwell, S. E., & Gordon, I. R. (2001). A comparison of statistical methods for meta-
575	analysis. Statistics in Medicine, 20(6), 825-840. https://doi.org/10.1002/sim.650
576	Cadotte, M. W., Mehrkens, L. R., & Menge, D. N. L. (2012). Gauging the impact of meta-
577	analysis on ecology. Evolutionary Ecology, 26(5), 1153–1167.
578	https://doi.org/10.1007/s10682-012-9585-z
579	Canty, A., & Ripley, A. (2017). boot: Bootstrap R (S-Plus) Functions (Version R package
580	version 1.3-20).
581	Gates, S. (2002). Review of methodology of quantitative reviews using meta-analysis in
582	ecology. Journal of Animal Ecology, 71(4), 547–557.
583	https://doi.org/10.1046/j.1365-2656.2002.00634.x
584	Gelman, A. (2004) Parameterization and Bayesian modeling. Journal of the American
585	Statistical Association, 99(466), 537–545
586	Gelman, A. (2006). Prior distributions for variance parameters in hierarchical models.
587	Bayesian Analysis, 1(3), 515–533.
588	Gelman, A., & Rubin, D. B. (1992). Inference from iterative simulation using multiple
589	sequences. Statistical Science, 7(4), 457-472.
590	https://doi.org/10.1214/ss/1177011136
591	Gurevitch, J., & Hedges, L. V. (1999). Statistical issues in ecological meta-analyses.
592	<i>Ecology</i> , 80(4), 1142–1149.

593	Gurevitch, J., Morrow, L. L., Wallace, A., & Walsh, J. S. (1992). A meta analysis of
594	competition in field experiments. The American Naturalist, 140(4), 539-572.
595	https://doi.org/10.1086/285428
596	Halekoh, U. & Hojsgaard, S. (2014). A Kenward-Roger approximation and parametric
597	bootstrap methods for tests in linear mixed models – the R package pbkrtest.
598	Journal of Statistical Software, 59(9), 1-32. https://doi.org/10.18637/jss.v059.i09
599	Hartung, J., & Knapp, G. (2001). A refined method for the meta-analysis of controlled
600	clinical trials with binary outcome. Statistics in Medicine, 20(24), 3875-3889.
601	https://doi.org/10.1002/sim.1009
602	Hedges, L. V., Gurevitch, J., & Curtis, P. S. (1999). The meta-analysis of response ratios in
603	experimental ecology. <i>Ecology</i> , 80(4), 1150. <u>https://doi.org/10.2307/177062</u>
604	Hesterberg, T. C. (2015). What teachers should know about the bootstrap: resampling in the
605	undergraduate statistics curriculum, The American Statistician, 69(4), 371-386
606	Higgins, J. P. T., Thompson, S. G., & Spiegelhalter, D. J. (2009). A re-evaluation of
607	random-effects meta-analysis. Journal of the Royal Statistical Society: Series A
608	(Statistics in Society), 172(1), 137-159. https://doi.org/10.1111/j.1467-
609	985X.2008.00552.x
610	Hillebrand, H., & Gurevitch, J. (2014). Meta-analysis results are unlikely to be biased by
611	differences in variance and replication between ecological lab and field studies.
612	Oikos, 123(7), 794–799. https://doi.org/10.1111/oik.01288

613 IntHout, J., Ioannidis, J. P., & Borm, G. F. (2014). The Hartung-Knapp-Sidik-Jonkman
614 method for random effects meta-analysis is straightforward and considerably

615	outperforms the standard DerSimonian-Laird method. BMC Medical Research
616	Methodology, 14(1). https://doi.org/10.1186/1471-2288-14-25
617	Kontopantelis, E., Springate, D. A., & Reeves, D. (2013). A re-analysis of the Cochrane
618	library data: the dangers of unobserved heterogeneity in meta-analyses. PLoS ONE,
619	8(7), e69930. https://doi.org/10.1371/journal.pone.0069930
620	Kruschke, J.K. & Liddell, T.M. (2018). The Bayesian new statistics: hypothesis testing,
621	estimation, meta-analysis, and power analysis from a Bayesian perspective.
622	Psychonomic Bulletin & Review, 25, 178-206. https://doi.org/10.3758/s13423-016-
623	1221-4
624	Lajeunesse, M. J. (2015). Bias and correction for the log response ratio in ecological meta-
625	analysis. Ecology, 96(8), 2056–2063. https://doi.org/10.1890/14-2402.1
626	Langan, D., Higgins, J. P. T., & Simmonds, M. (2016). Comparative performance of
627	heterogeneity variance estimators in meta-analysis: a review of simulation studies.
628	Research Synthesis Methods 8(2), 181-198. https://doi.org/10.1002/jrsm.1198
629	Luke, S.G. (2017). Evaluating significance in linear mixed-effect models in R. Behavior
630	Research Methods, 49, 1494-1502. https://doi.org/10.3758/s13428-016-0809-y
631	Nakagawa, S., & Santos, E. S. A. (2012). Methodological issues and advances in biological
632	meta-analysis. Evolutionary Ecology, 26(5), 1253–1274.
633	https://doi.org/10.1007/s10682-012-9555-5
634	Nakagawa, S., Noble, D. W., Senior, A.M. & Lagisz, M. (2017). Meta-evaluation of meta-
635	analysis: ten appraisal questions for biologists. BMC Biology, 15:18.
636	https://doi.org/10.1186/s12915-017-0357-7

637	Noble, D. W. A., Lagisz, M., O'dea, R. E., & Nakagawa, S. (2017). Nonindependence and
638	sensitivity analyses in ecological and evolutionary meta-analyses. Molecular
639	Ecology, 26(9), 2410–2425. https://doi.org/10.1111/mec.14031
640	Ogle, K., Barber, J., & Sartor, K. (2013). Feedback and Modularization in a Bayesian
641	Meta-analysis of Tree Traits Affecting Forest Dynamics. Bayesian Analysis, 8(1),
642	133-168. https://doi.org/10.1214/13-BA806
643	Osenberg, C. W., Sarnelle, O., & Cooper, S. D. (1997). Effect size in ecological
644	experiments: the application of biological models in meta-analysis. The American
645	Naturalist, 150(6), 798–812.
646	Osenberg, C. W., Sarnelle, O., Cooper, S. D., & Holt, R. D. (1999). Resolving ecological
647	questions through meta-analysis: goals, metrics, and models. Ecology, 80(4), 1105-
648	1117.
649	Pappalardo, P. K. Ogle, E.A. Hamman, J.R. Bence, B.A. Hungate, & C.W. Osenberg.
650	(2020). Data from: Comparing traditional and Bayesian approaches to ecological
651	meta-analysis. Methods in Ecology and Evolution doi:/10.5061/dryad.zw3r22863
652	Plummer, M. (2018). rjags: Bayesian Graphical Models using MCMC (Version R package
653	version 4-8.).
654	R Core Team. (2019). R: A language and environment for statistical computing. Vienna,
655	Austria.: R Foundation for Statistical Computing.
656	Sánchez-Meca, J., & Marín-Martínez, F. (2008). Confidence intervals for the overall effect
657	size in random-effects meta-analysis. Psychological Methods, 13(1), 31-48.
658	https://doi.org/10.1037/1082-989X.13.1.31

660	of invasive plants on resident animals across ecosystems, taxa, and feeding types: a
661	global assessment. Global Change Biology, 22(2), 594-603.
662	https://doi.org/10.1111/gcb.13093
663	Schmid, C. H., & Mengersen, K. (2013). Bayesian meta-analysis. In Handbook of meta-
664	analysis in ecology and evolution (pp. 145–173). Princeton, New Jersey: Princeton
665	University Press.
666	Senior, A. M., Grueber, C. E., Kamiya, T., Lagisz, M., O'Dwyer, K., Santos, E. S. A., &
667	Nakagawa, S. (2016). Heterogeneity in ecological and evolutionary meta-analyses:
668	its magnitude and implications. Ecology, 97(12), 3293-3299.
669	https://doi.org/10.1002/ecy.1591
670	Sidik, K., & Jonkman, J. N. (2003). On constructing confidence intervals for a standardized
671	mean difference in meta-analysis. Communications in Statistics - Simulation and
672	Computation, 32(4), 1191-1203. https://doi.org/10.1081/SAC-120023885
673	Sundar, DR. (2014). binom: binomial confidence intervals for several parameterizations
674	(Version R package version 1.1-1).
675	Song, C., Peacor, S.D., Osenberg, C.W., & Bence, J.R. (2020). An assessment of statistical
676	methods for non-independent data in ecological meta-analyses. Ecology (under
677	review).
678	Thébault, A., Mariotte, P., Lortie, C. J., & MacDougall, A. S. (2014). Land management
679	trumps the effects of climate change and elevated CO $_2$ on grassland functioning.
680	Journal of Ecology, 102(4), 896–904. https://doi.org/10.1111/1365-2745.12236

Schirmel, J., Bundschuh, M., Entling, M. H., Kowarik, I., & Buchholz, S. (2016). Impacts

681	Viechtbauer, W. (2007). Confidence intervals for the amount of heterogeneity in meta-
682	analysis. Statistics in Medicine, 26(1), 37-52. https://doi.org/10.1002/sim.2514

683 Viechtbauer, W. (2010). Conducting Meta-Analyses in R with the metafor Package.

*Journal of Statistical Software*, *36*(3). https://doi.org/10.18637/jss.v036.i03

685

# 686 FIGURE LEGENDS

**Figure 1**. Results from the literature review of ecological meta-analyses: A) distribution of the number of studies (*k*) reported for overall, analysis, and category levels; the median *k* is indicated in each panel; B) distribution of the number of replicates used in the original studies ( $n_i$ ), as reported in each meta-analysis; the median  $n_i$  is indicated with a dashed line. Note that the x-axes are on a log scale.

692

Figure 2. Types of uncertainty intervals reported by the ecological meta-analyses. In somecases, more than one type of uncertainty interval was reported.

695

**Figure 3**. Coverage and the width of the 95% uncertainty interval for different methods used to estimate the mean effect size ( $\mu$ ) in a meta-analysis as a function of the number of studies (A, D), the mean number of replicates (B, E), and the among-study variance (C, F). The dashed horizontal line in panels A, B, and C indicates the nominal value of 95%. Different colors denote the method used to estimate the uncertainty interval. Error bars provide the 95% CI.

702

#### 703 SUPPLEMENTARY FIGURE LEGENDS

704

**Figure S1**. PRISMA diagram.

Figure S2. Mean  $I^2$  as a function of the true (simulated) among-study variance for different combinations of the mean number of replicates,  $n_i$ , and number of studies, k, in the simulated datasets.

Figure S3. Number of climate-change meta-analyses reviewed, summarized by journal in
which each was published, between 2013 and 2016.

Figure S4. Results from the exploratory literature search on sub-disciplines of ecological meta-analyses. A) distribution of the number of studies (k) by sub-discipline; B) distribution of the number of replicates ( $n_i$ ) used in the primary papers, as reported in each meta-analysis. Replication was not reported in any meta-analyses for ocean acidification. Note that the xaxes are on a log scale.

Figure S5. Additional results for the climate/global change meta-analysis. Variability on the
median number of studies at the analysis level (A) and the median number of replicates (B)
by type of organism (or variable) measured, type of environment, and meta-analysis topic.

**Figure S6**. Distribution of the number of replicates,  $n_i$ , in the original studies for each of the 26 meta-analysis publications in our review that provided the original data. The boxplots represent the median (thick vertical line), the 25<sup>th</sup> and 75<sup>th</sup> percentiles (box), the upper whisker extends from the box to the larger value no further than 1.5xIQR, and the lower whisker extends from the box to the smallest value at most 1.5xIQR. Extreme values that exceed the whiskers are plotted individually as solid points. 725 Figure S7. Performance measures of the estimation of the among-study variance as a 726 function of the number of studies (left column), the number of replicates in the original 727 studies (middle column) and the simulated among-study variance (right column). 728 Performance was assessed using coverage (A, B, C), perceived uncertainty (width of the 729 uncertainty interval) (D, E, F), bias (G, H, I), and RMSE (J, K, L). Error bars provide the 95% CI for panels A-I. Please note different scales in the y-axis for bias and width of the 730 uncertainty interval. Simulation parameters:  $n = 5, k = 25, \sigma_{among}^2 = 0.5$ , except for the 731 cases in which that parameter was varied. 732

Figure S8. Performance measures of the estimation of the among-study variance as a 733 734 function of the number of studies (left column), the number of replicates in the original 735 studies (middle column) and the simulated among-study variance (right column). Performance was assessed using coverage (A, B, C), perceived uncertainty (width of the 736 uncertainty interval) (D, E, F), bias (G, H, I), and RMSE (J, K, L). Error bars provide the 737 95% CI for panels A-I. Please note different scales in the y-axis for bias and width of the 738 uncertainty interval. Simulation parameters:  $n = 5, k = 25, \sigma_{among}^2 = 2$ , except for the cases 739 in which that parameter was varied. 740

**Figure S9**. Performance measures of the estimation of the among-study variance as a function of the number of studies (left column), the number of replicates in the original studies (middle column) and the simulated among-study variance (right column). Performance was assessed using coverage (A, B, C), perceived uncertainty (width of the uncertainty interval) (D, E, F), bias (G, H, I), and RMSE (J, K, L). Error bars provide the 95% CI for panels A-I. Please note different scales in the y-axis for bias and width of the uncertainty interval. Simulation parameters:  $n = 20, k = 25, \sigma_{among}^2 = 2$ , except for the cases in which that parameter was varied.

749 Figure S10. Performance measures of the estimation of the among-study variance as a 750 function of the number of studies (left column), the number of replicates in the original studies (middle column) and the simulated among-study variance (right column). 751 Performance was assessed using coverage (A, B, C), perceived uncertainty (width of the 752 uncertainty interval) (D, E, F), bias (G, H, I), and RMSE (J, K, L). Error bars provide the 753 754 95% CI for panels A-I. Please note different scales in the y-axis for bias and width of the uncertainty interval. Simulation parameters:  $n = 20, k = 25, \sigma_{among}^2 = 0.5$ , except for the 755 cases in which that parameter was varied. 756

**Figure S11**. Bias and RMSE from the estimation of a mean effect in 2000 replicated metaanalyses as a function of the number of studies (A, B), the mean number of replicates in the original studies (C, D), and the among-study variance (E, F). Simulation parameters: n = $5, k = 25, \sigma_{among}^2 = 2$ , except for the cases in which that parameter was varied. Error bars provide the 95% CI for panels A-E.

**Figure S12**. Number of replicates yielding bad  $\hat{R}$  ( $\hat{R} \ge 1.1$ ) for different combinations of priors, true among-study variance, mean number of replicates, and number of studies.

Figure S13. Median of the posterior distribution of the among-study variance for all the different priors tested, number of replicates, number of studies, and true among-study variance. A) n = 5; B) n = 25. The vertical dashed line in each panel indicates the true among-study variance. **Figure S14**. Median of the posterior distribution of the among-study variance for the four priors with the best performance (i.e., Uniform (0, 10), Uniform (0, 100), Gamma, Foldedt), number of replicates, number of studies, and true among-study variance. A) n = 5; B)

- n = 25. The vertical dashed line in each panel indicates the true among-study variance.
- **Figure S15**. Median of the posterior distribution of the among-study variance for the four
- priors with the best performance (i.e., Uniform (0, 10), Uniform (0, 100), Gamma, Folded-
- t), when the number of studies was low (k = 5). A) n = 5; B) n = 25. The vertical dashed
- <sup>775</sup> line in each panel indicates the true among-study variance.